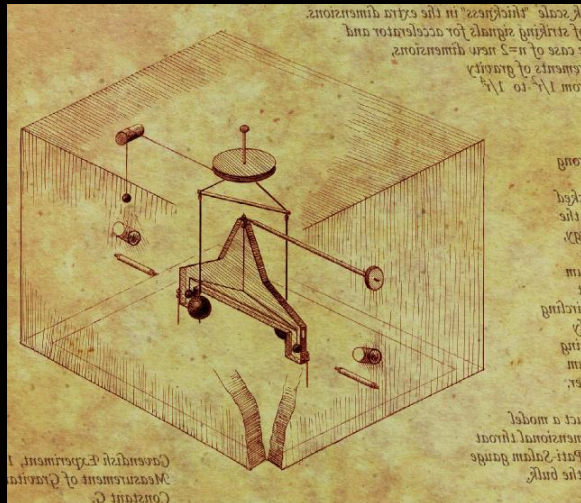


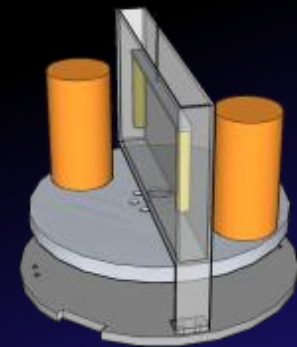


Short-Range Gravity experiment using digital image analysis

Test of Newtonian Inverse square law and weak equivalence principle



Rikkyo Univ./ RIKEN
Kazufumi Ninomiya



© Jiro Murata

Rikkyo Univ.^A RIKEN^B

N. Ogawa^A, R. Kishi^A, A. Taketani^B, Y. Nishio^A, H. Murakami^A
and J. Murata^A

Motivation

Why short-range Gravity?

Hierarchy problem

Gravity is extremely weak comparing to other 3 gauge interactions



Gravity propagates toward extra dimensions.

Large Extra Dimension model

(N. Arkani-Hamed et.. al.. PLB429(1998)263)

$$V(r) = -G_N \frac{mM}{r} \quad \lambda \leq r$$

$$V(r) = -G_{4+n} \frac{mM}{r^{1+n}} \quad \lambda \geq r$$

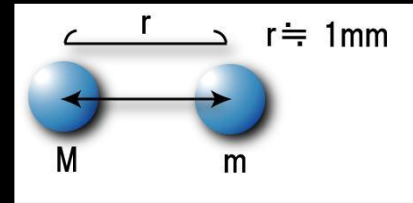
λ : interaction length

Past experiments

Parameterized by Yukawa potential

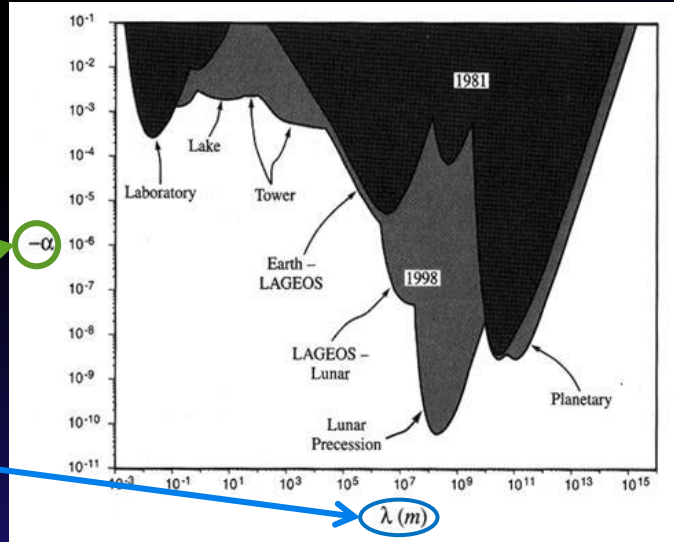
$$V(r) = -G \frac{mM}{r} \left(1 + \alpha e^{-\frac{r}{\lambda}} \right)$$

λ : interaction length
 α : coupling constant



Possibility of the deviation from gravitational inverse square law below mm scale

Limit on the new Yukawa interaction



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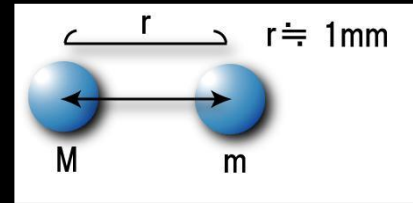
Past experiments

Parameterized by

$$V(r) = -G \frac{mM}{r} \left(1 + \alpha e^{-\frac{r}{\lambda}} \right)$$

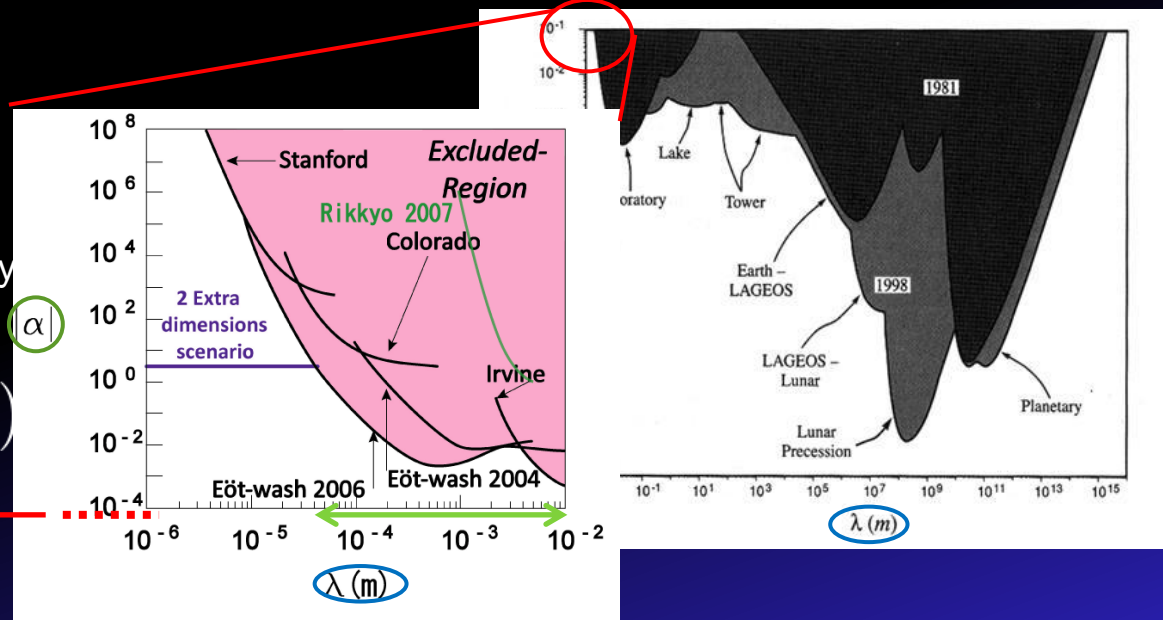
λ : interaction length
 α : coupling constant

MTV-G (~fm)



Possibility of the deviation from gravitational inverse square law below mm scale

Limit on the new Yukawa interaction



Principle

Torsion pendulum

$$\tau = -\kappa\delta\theta$$

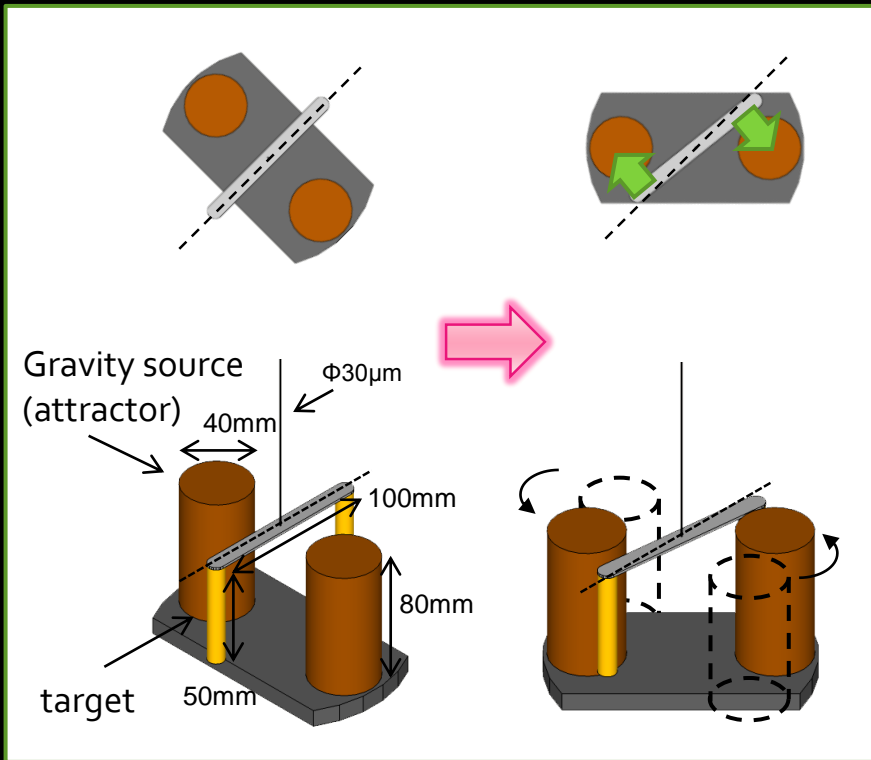
κ : Torsional spring constant

Torque \propto Angular Displacement

Angular displacement
of torsion pendulum

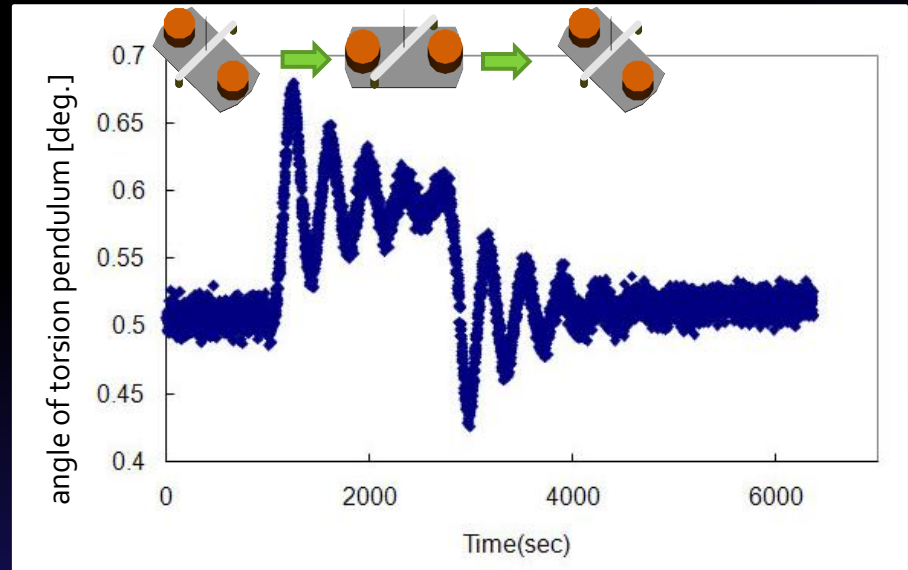


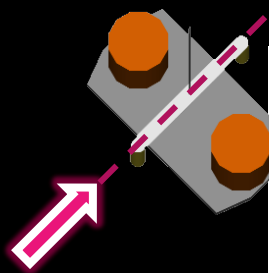
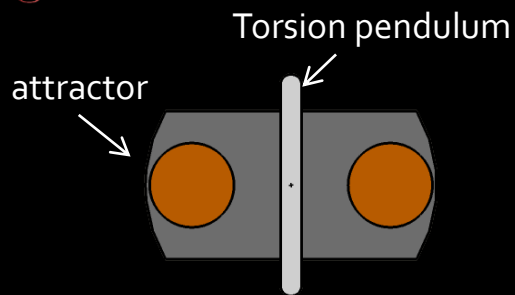
Gravitational signal
from attractor source



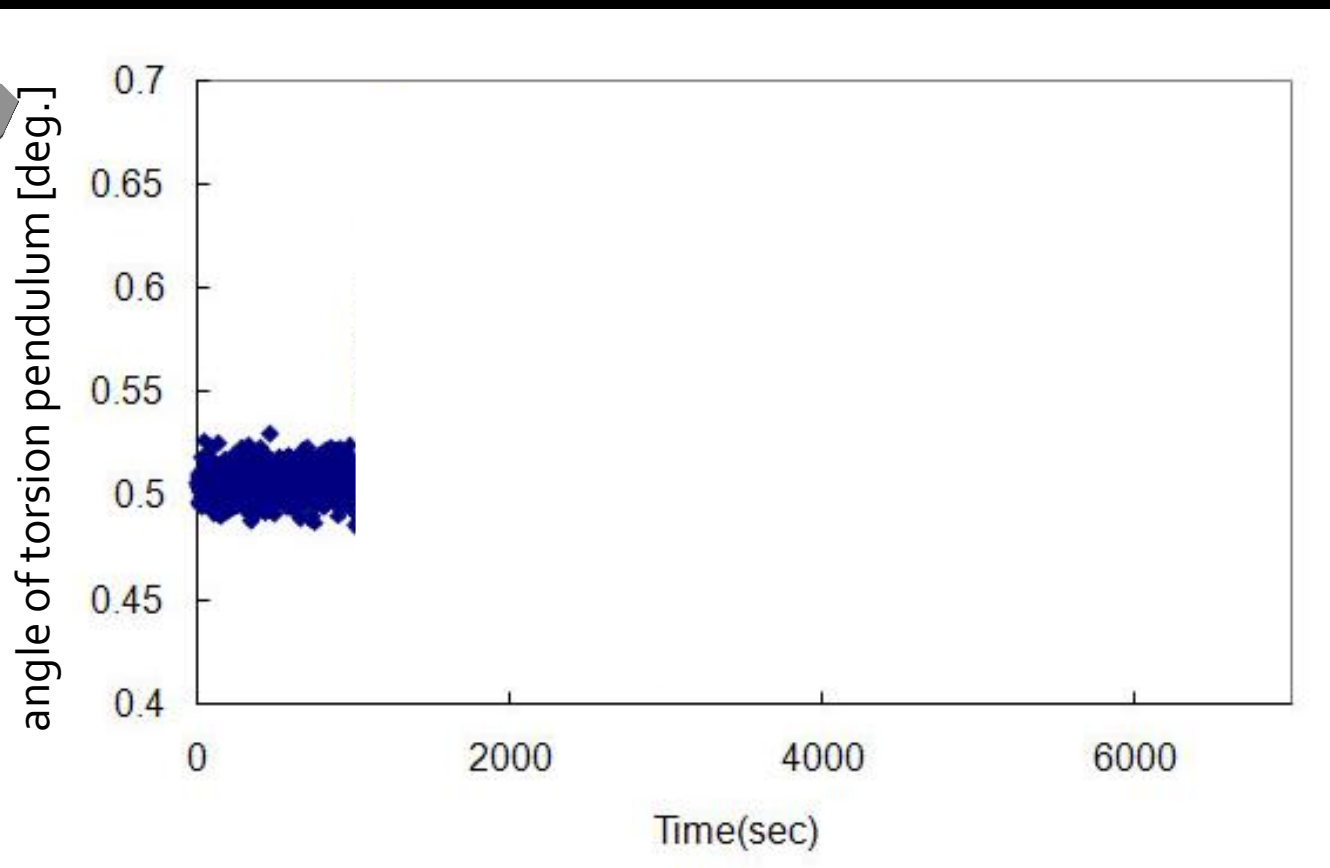
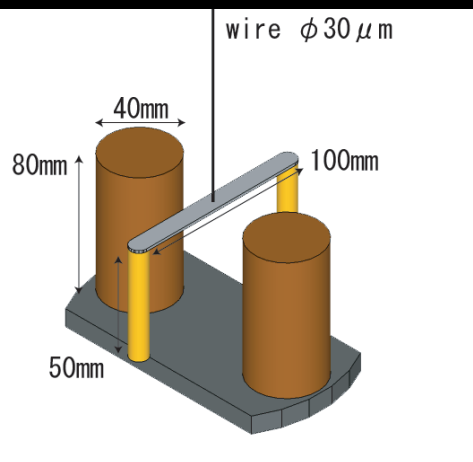
Measurement of the angular displacement

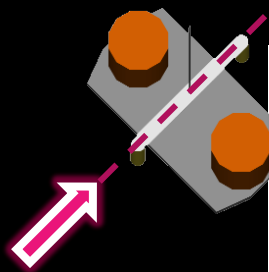
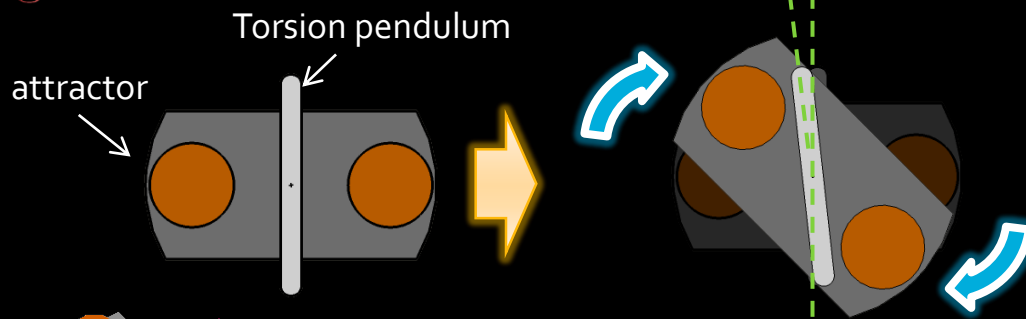
Our typical experimental data



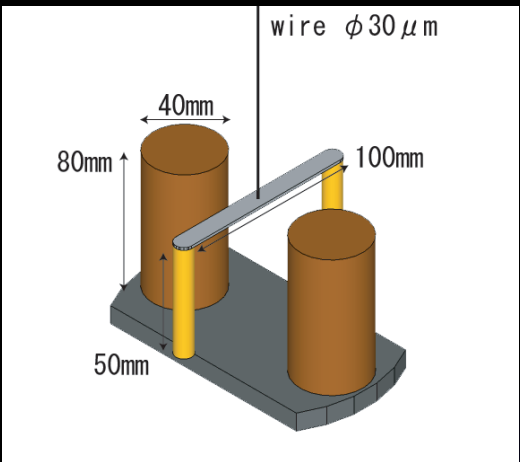
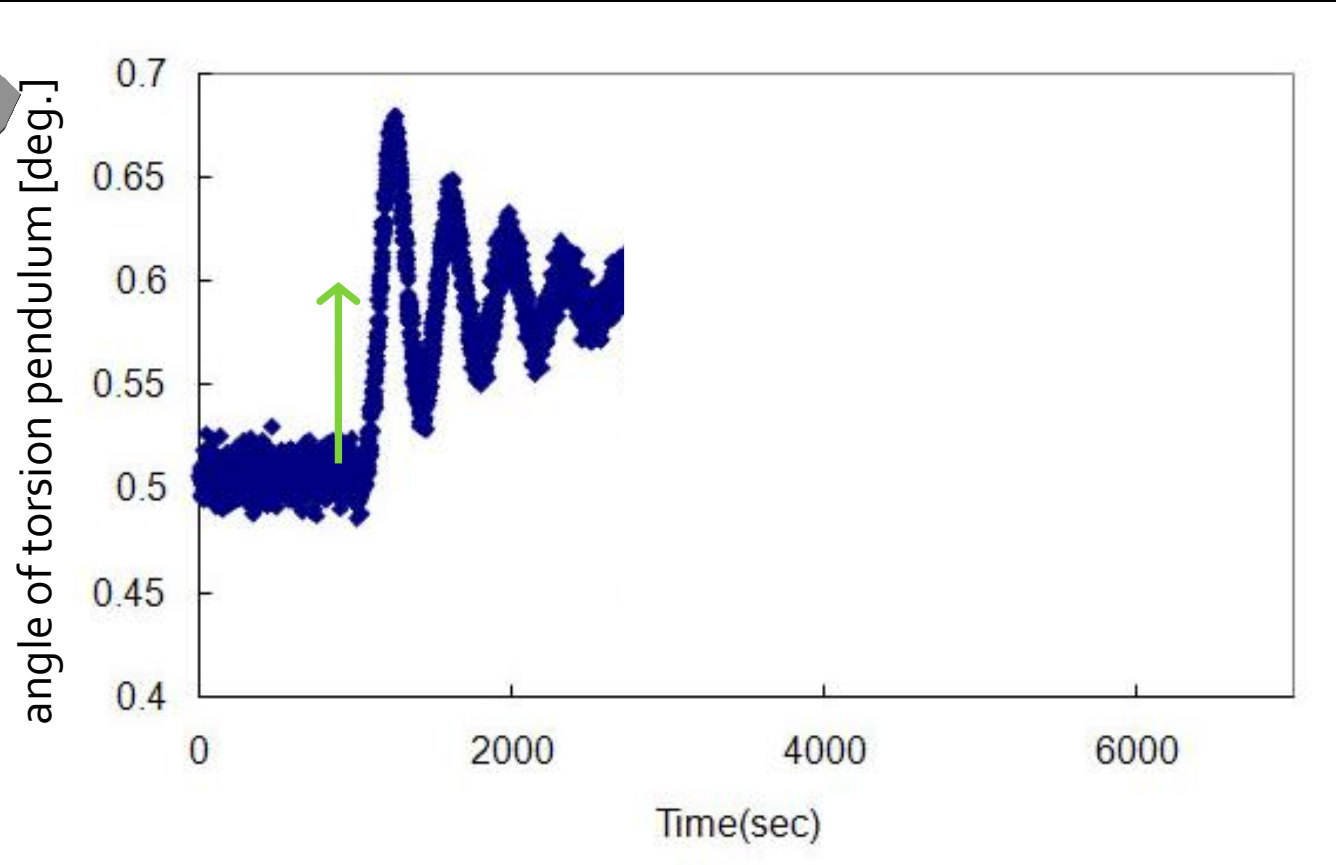


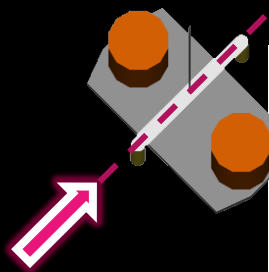
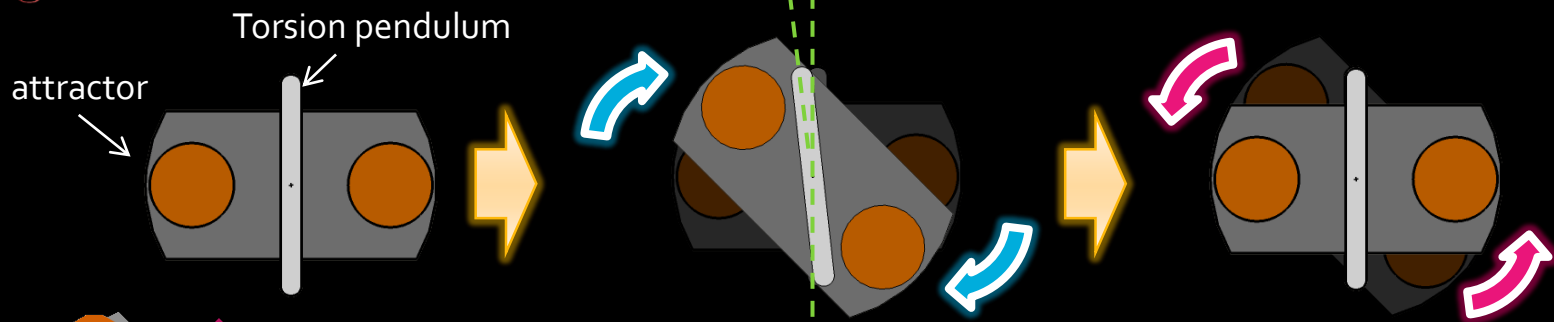
Torque
 \propto **Angular Displacement**



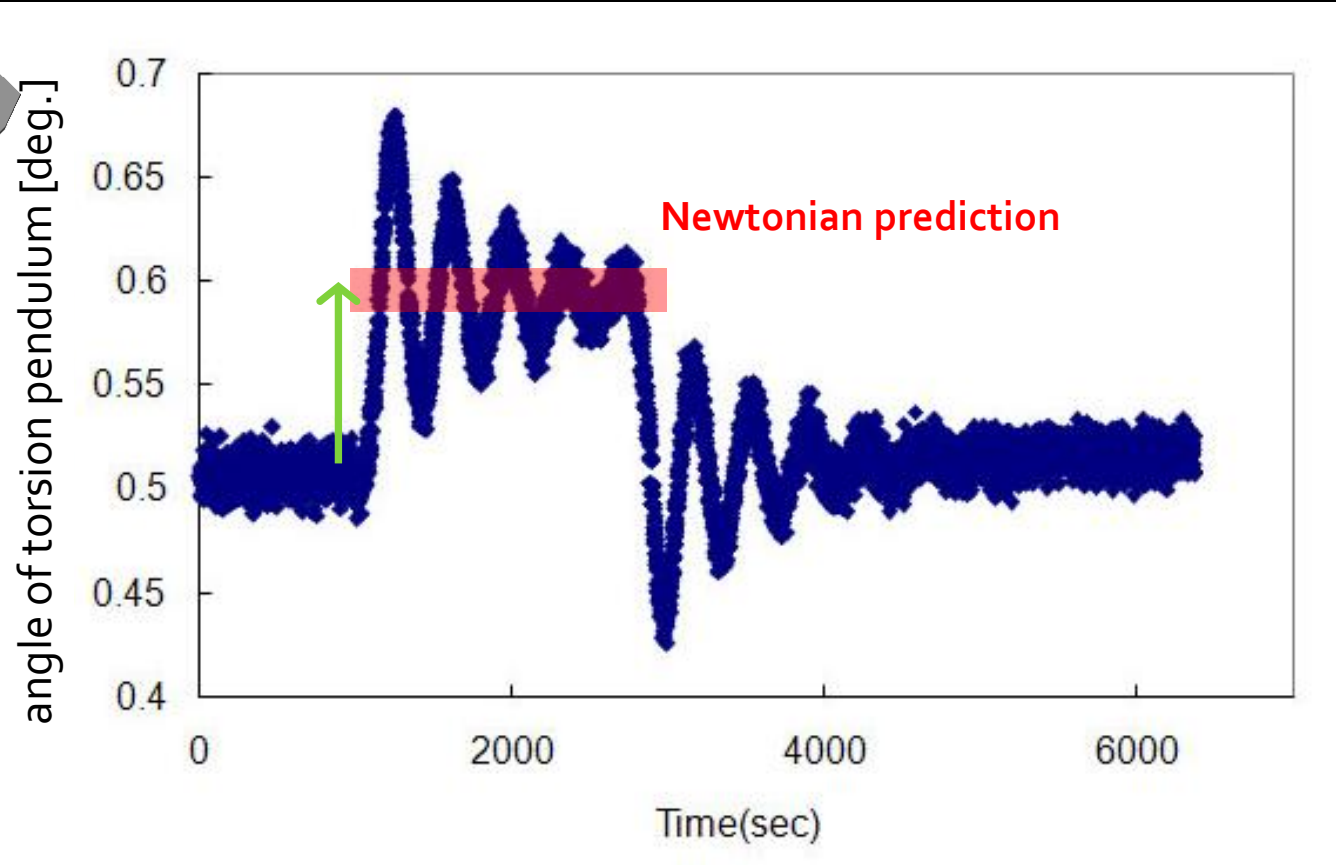
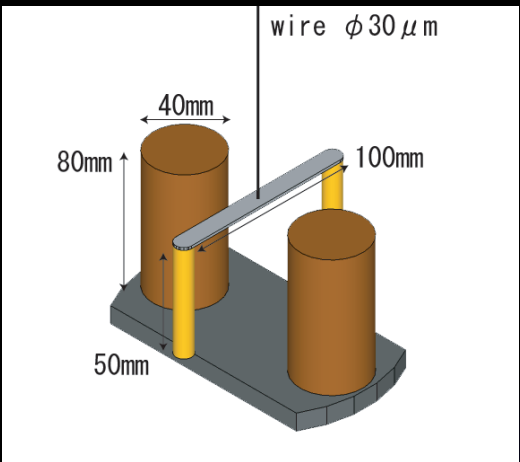


Torque
 \propto **Angular Displacement**

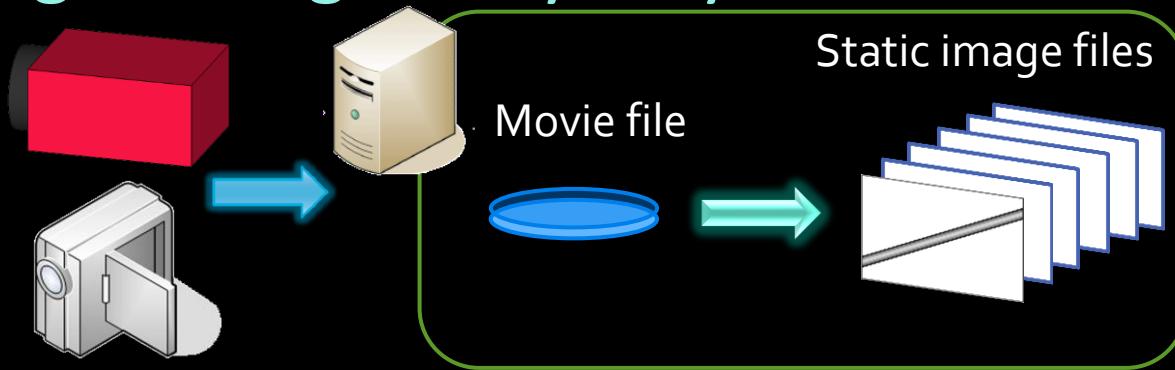




Torque
 \propto **Angular Displacement**



Digital Image analysis system

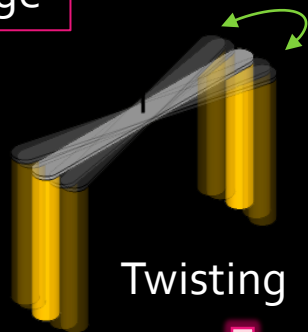


Determining of the angle of the torsion balance bar using pixel intensity

angular resolution : 1μ degree

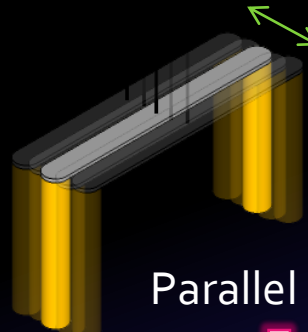
Offline analysis

Advantage



Twisting motion

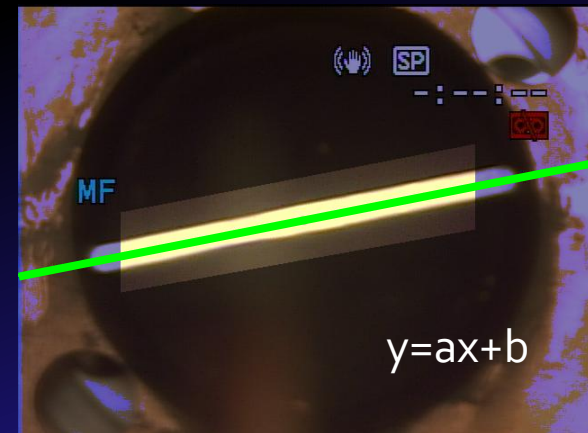
Signal



Parallel motion

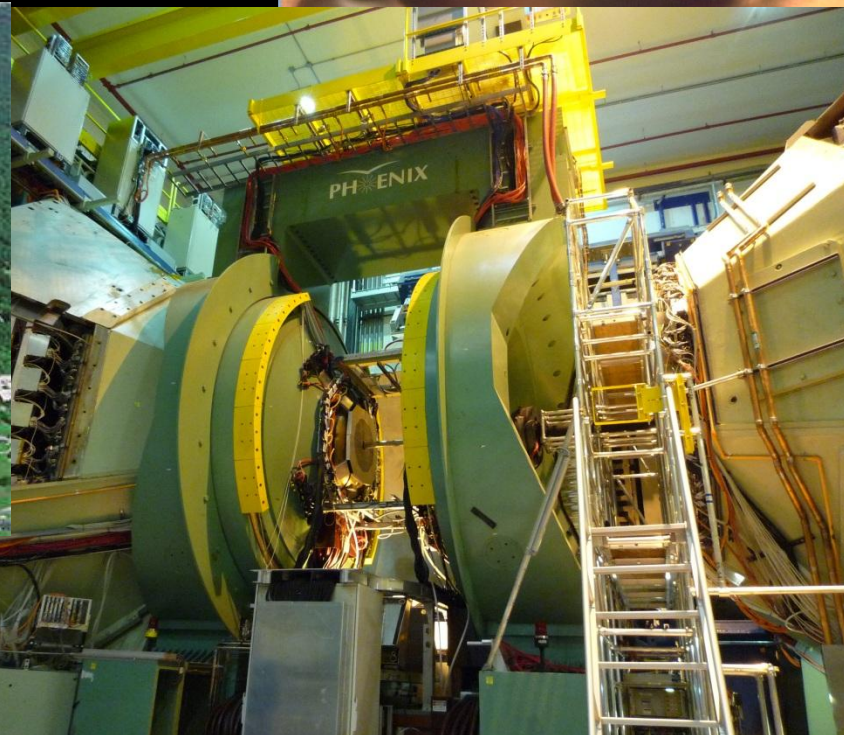
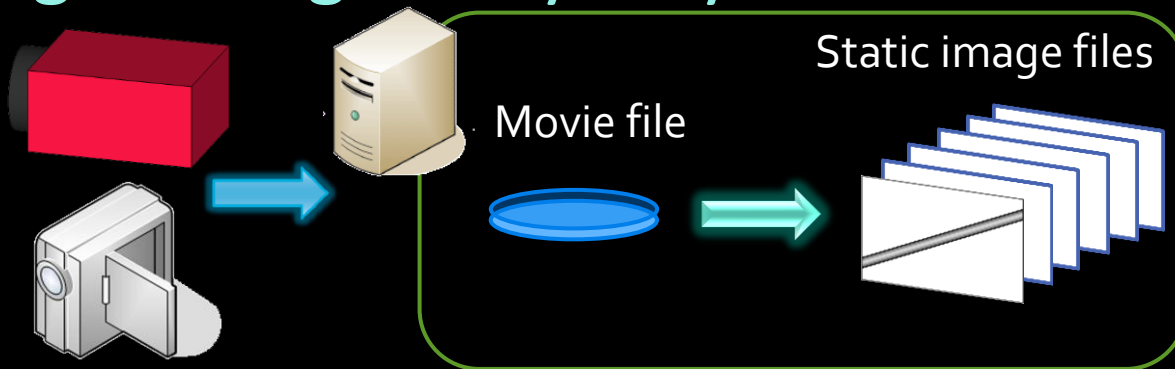
Fake signal

Suppression of the parallel motion





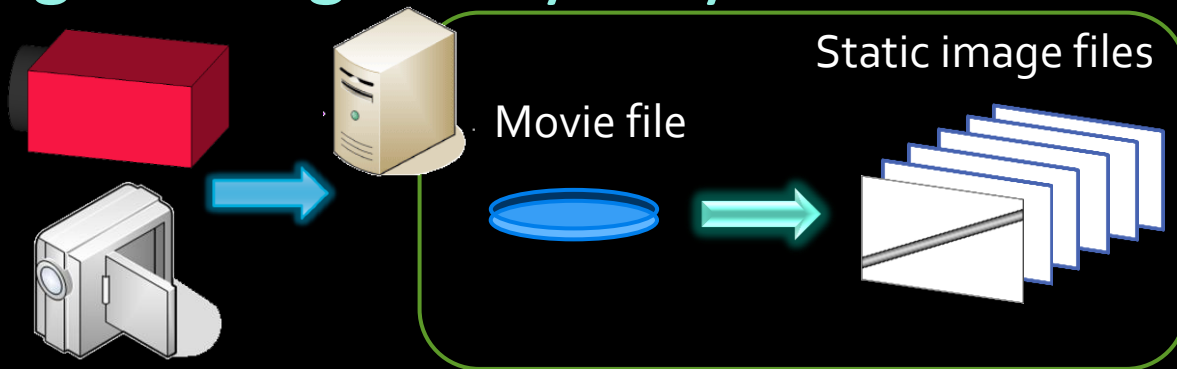
Digital Image analysis system



Signal

Suppression of the pa

Digital Image analysis system

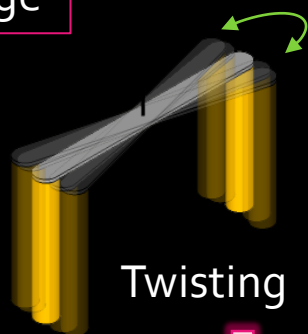


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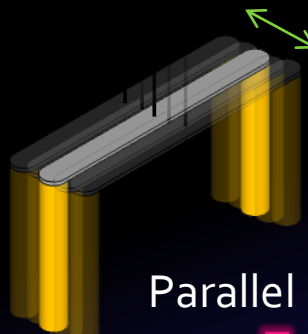
Offline analysis

Advantage



Twisting motion

Signal



Parallel motion

Fake signal

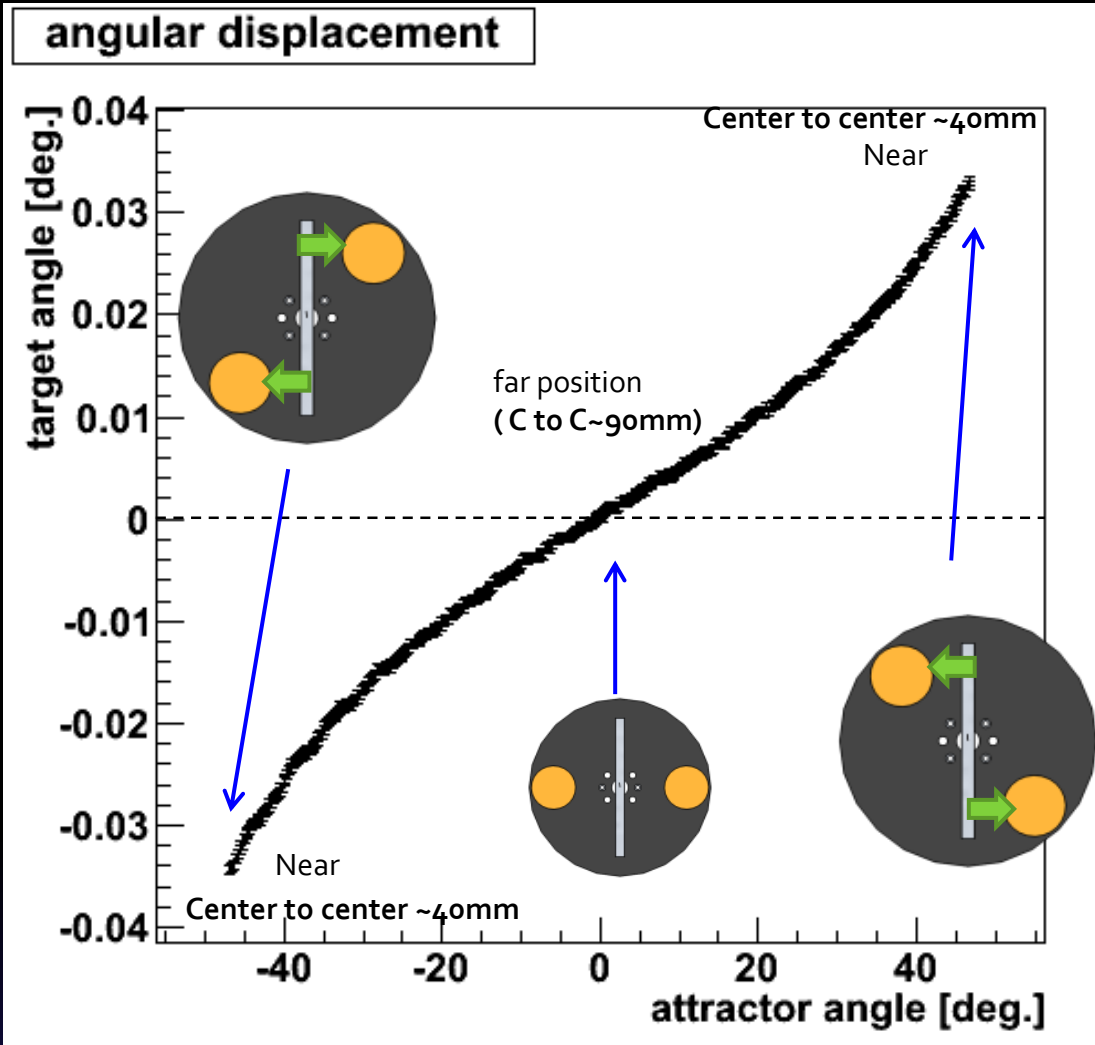
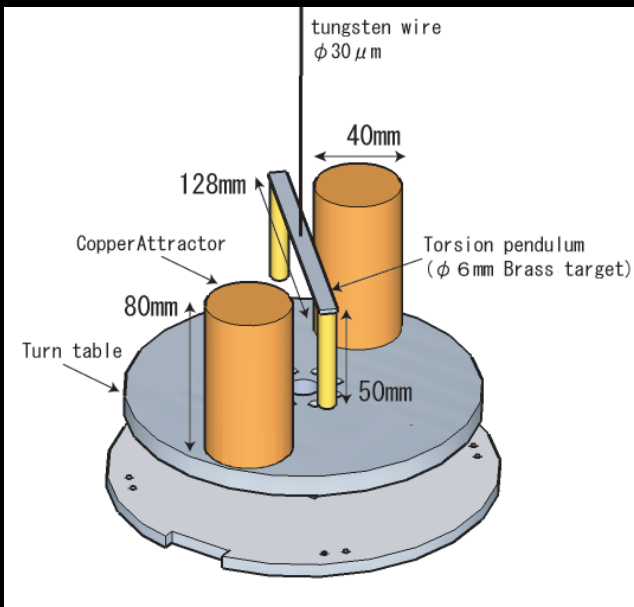
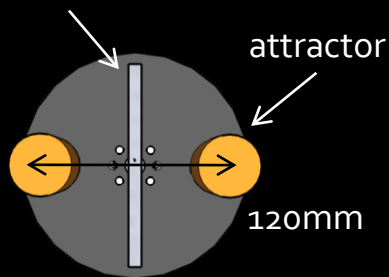
Suppression of the parallel motion



Gravitational Inverse Square Law

Experiment

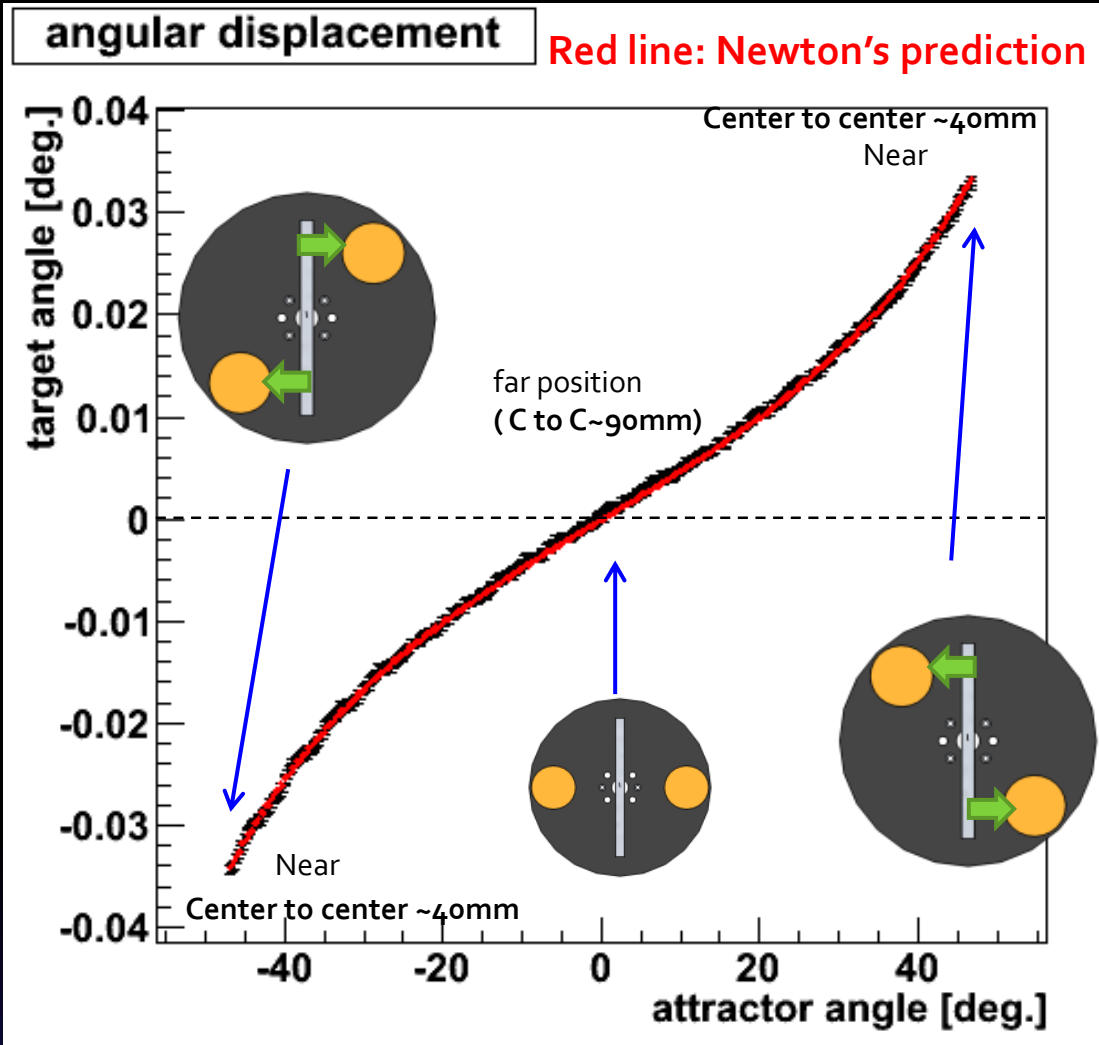
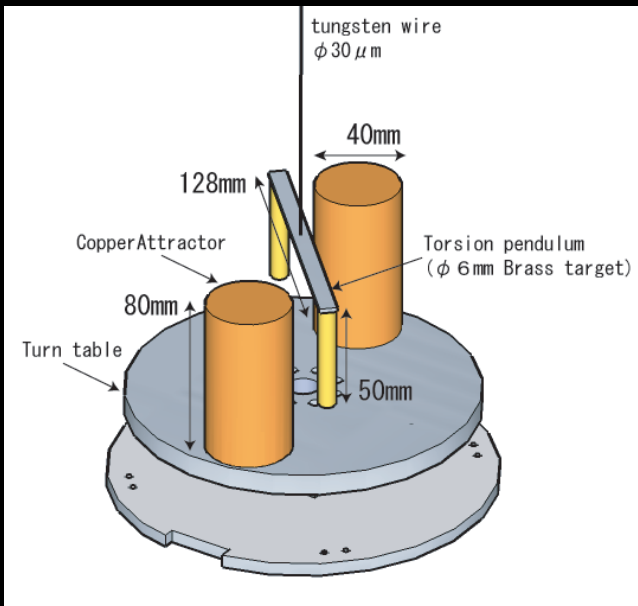
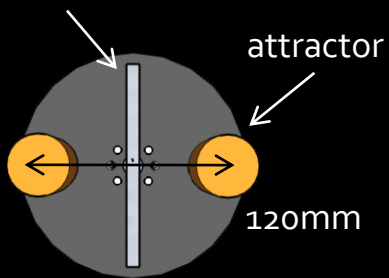
Torsion pendulum



Gravitational Inverse Square Law

Experiment

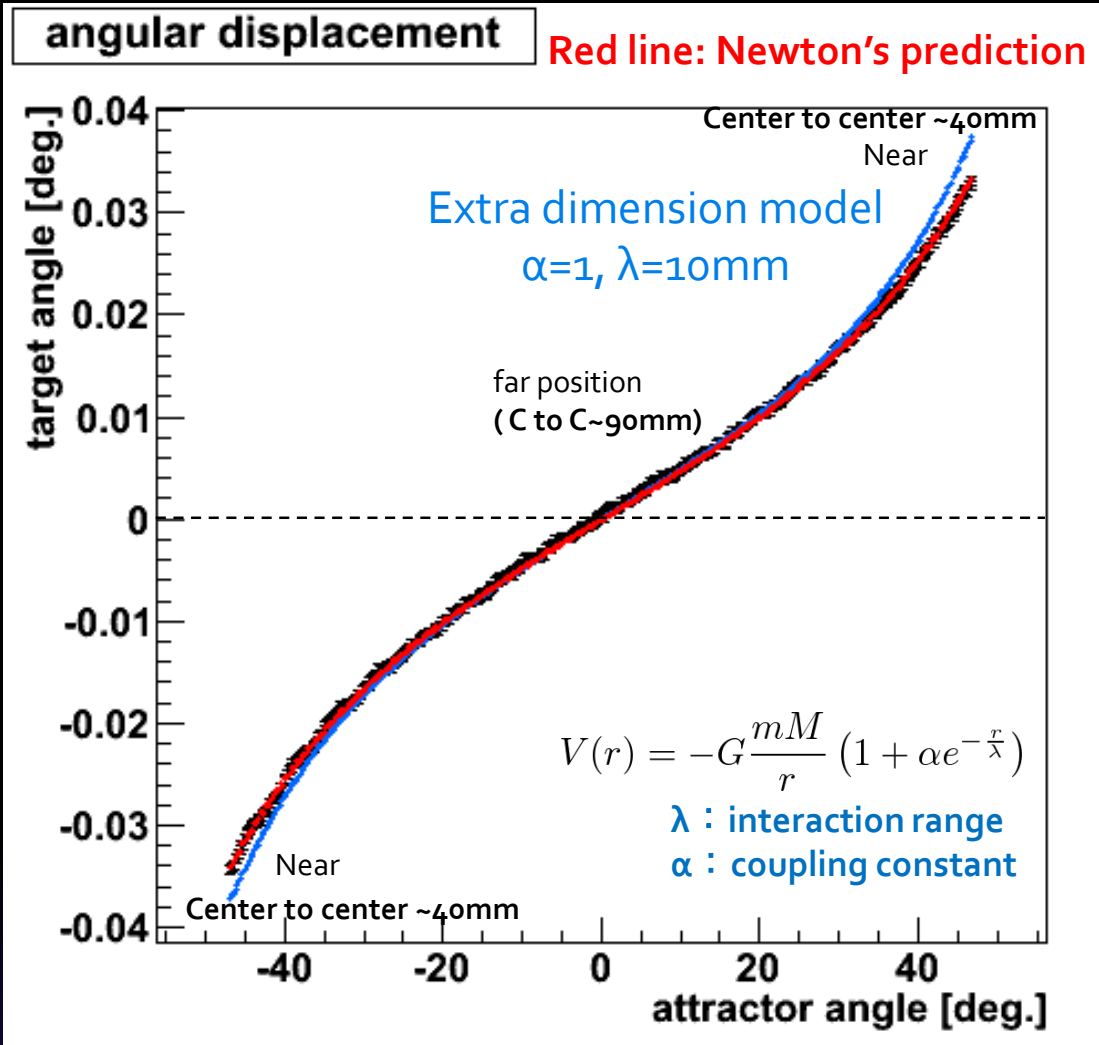
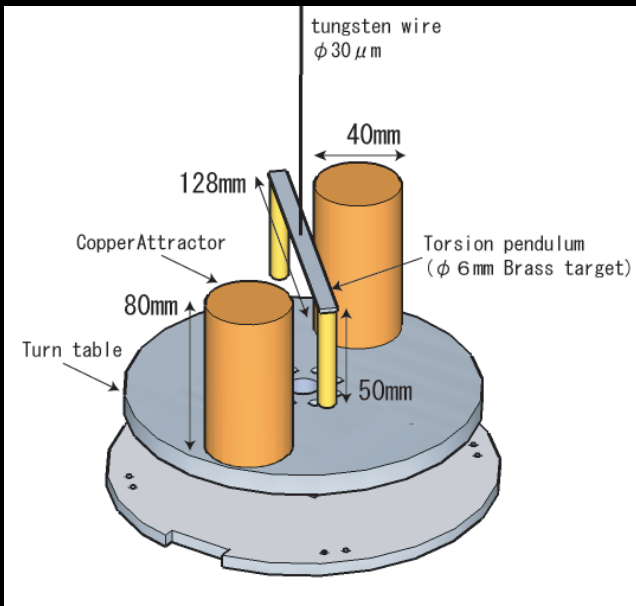
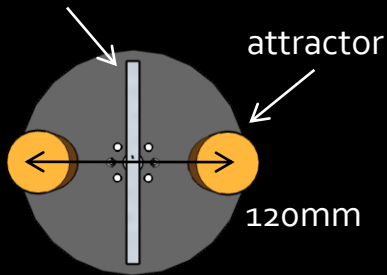
Torsion pendulum



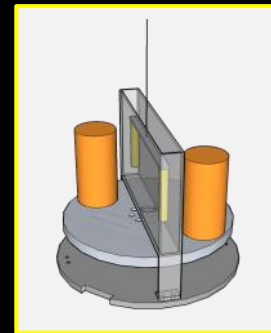
Gravitational Inverse Square Law

Experiment

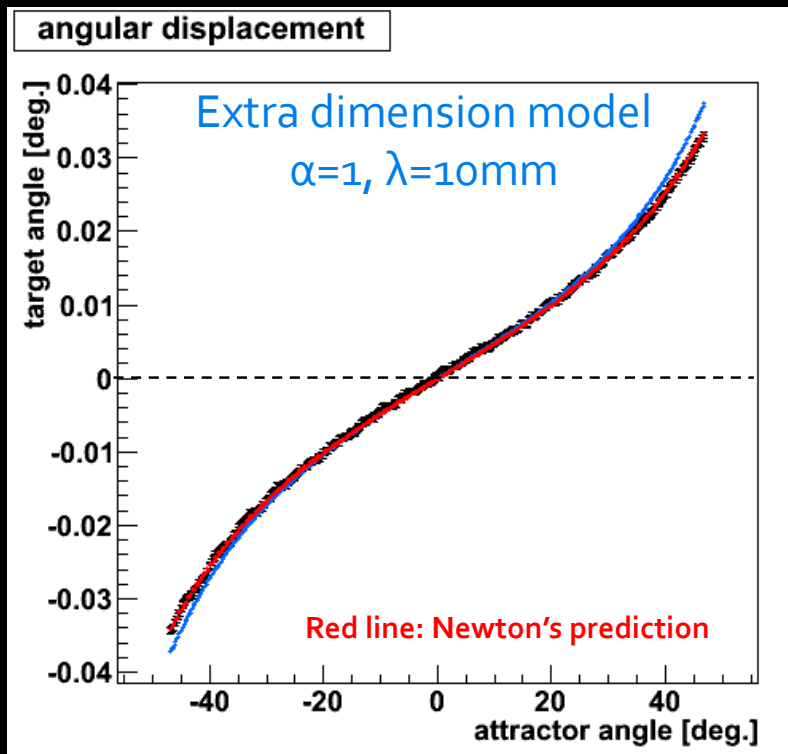
Torsion pendulum



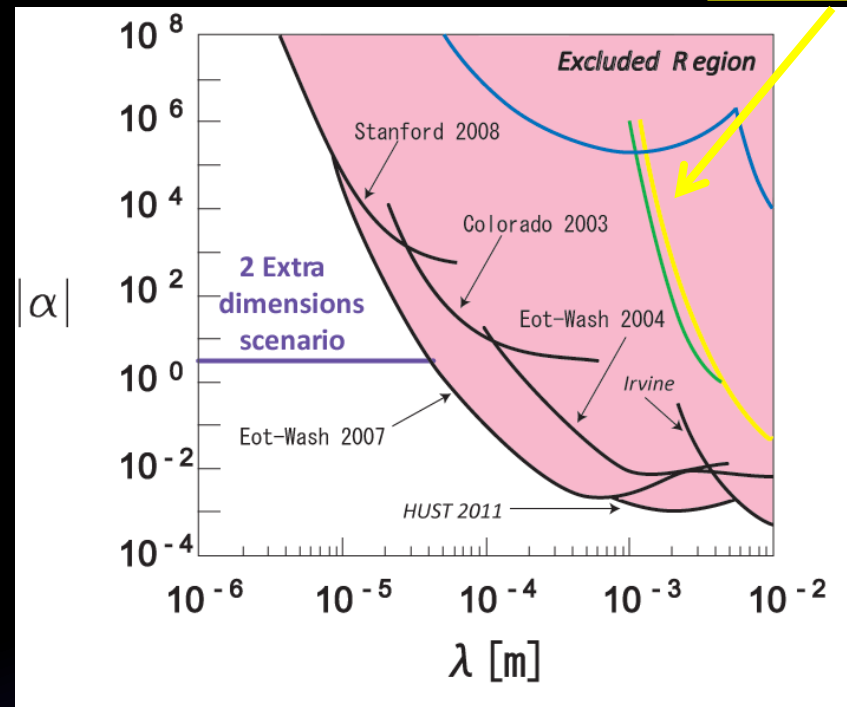
Gravitational Inverse Square Law



Our experimental result



Upper limit of the new Yukawa interaction

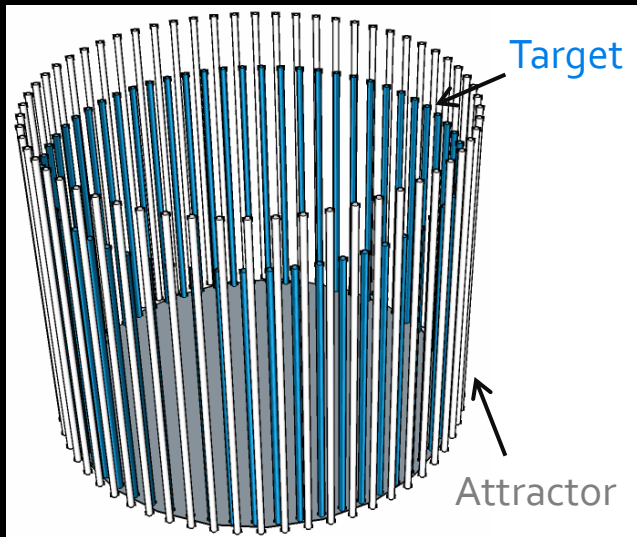


$$V(r) = -G \frac{mM}{r} \left(1 + \alpha e^{-\frac{r}{\lambda}} \right)$$

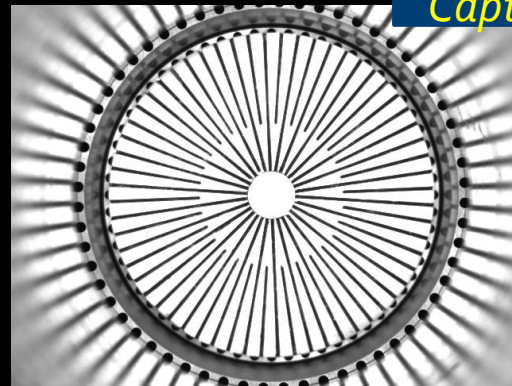
λ : interaction range

α : coupling constant

Next generation device

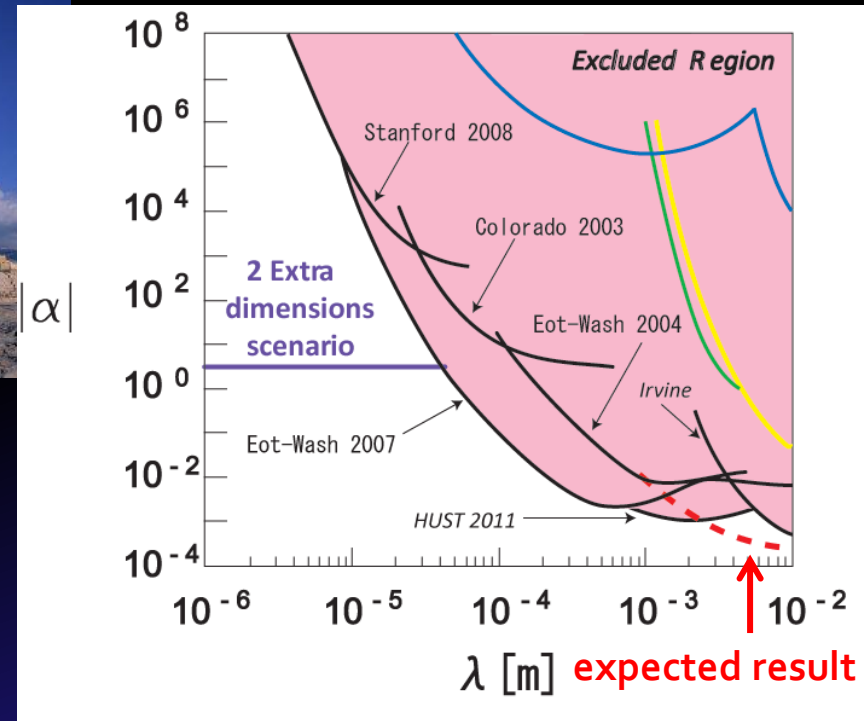


Center to center of 1.9 mm



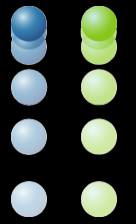
Capture Image

- NULL type experiment
- Suppression the systematic error



Composition dependence of gravitational constant G

Weak Equivalence Principle (WEP)



$$\frac{m_g}{m_I} = 1 + \kappa \quad (\kappa = \text{const.})$$

gravitational mass m_g
inertia mass m_I

Universality of the Free Fall



Test of WEP

Composition dependence of the gravitational constant

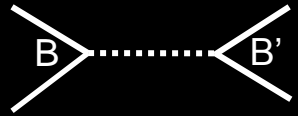
if WEP is violated...



Gravitational acceleration would have material dependence

$$\kappa_{ij} - \kappa_{ik} \neq 0$$

Model of WEPV



For example... Baryon number coupling force (BNC)
(Lee and Yang Phys. Rev. 98(1955))

Conservation of baryon number  Possibility of new interaction coupled baryon number

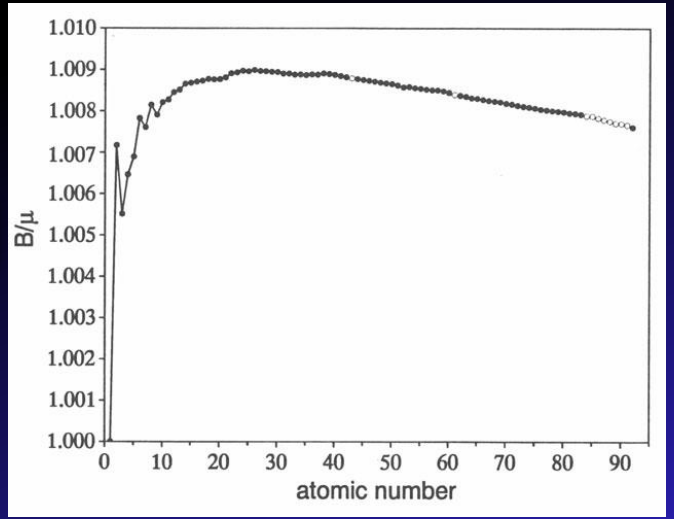
$$\text{nuclear mass} \sim \text{nucleon mass} \times \text{nucleon number}$$

Distinguishable BNC and Gravity, comparing with different ratios between baryon number and gravitational mass



atomic number dependence

Baryon number is dependence of Z



Composition dependence of gravitational constant G

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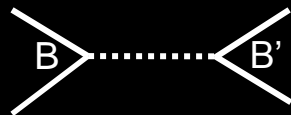
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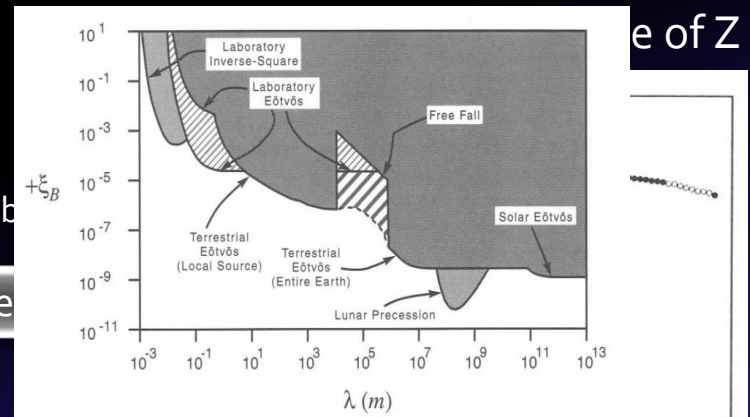
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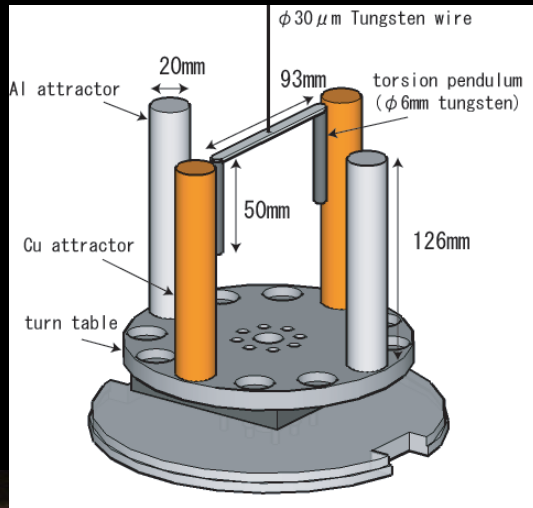
atomic number dependence

$$\kappa_{ij} - \kappa_{ik} \neq 0$$

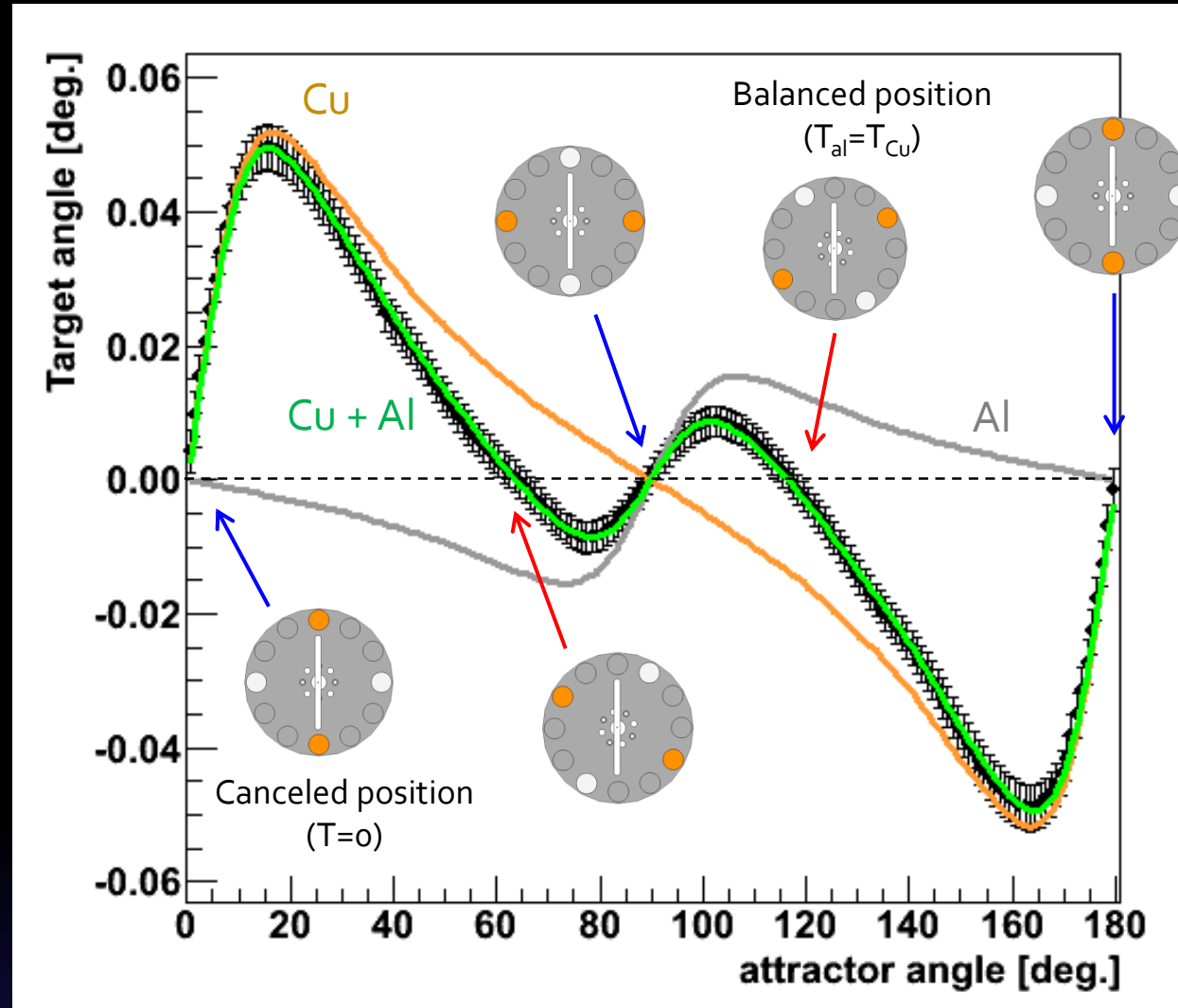


No direct experimental test at cm

Result



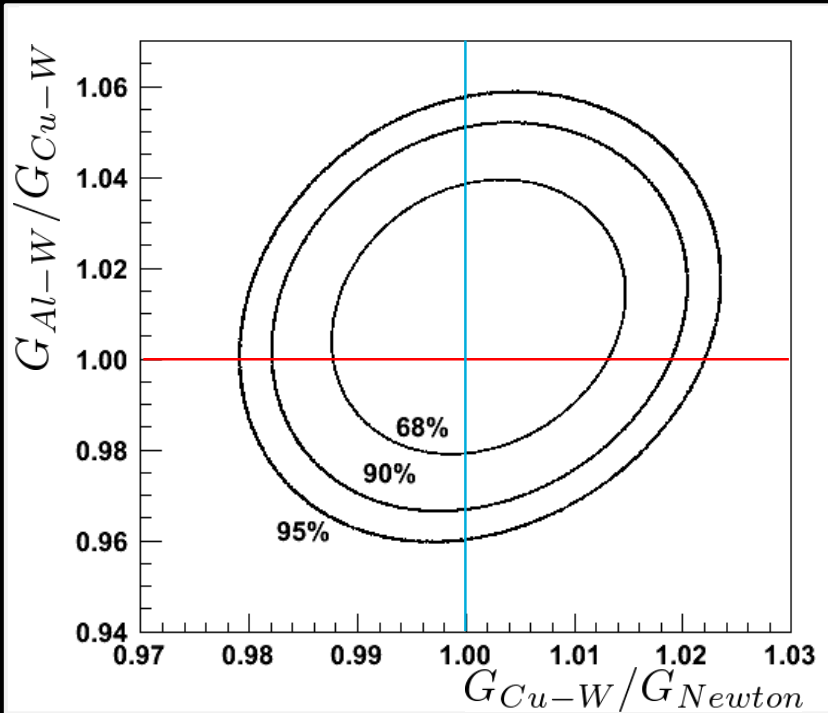
Torque \propto angular displacement





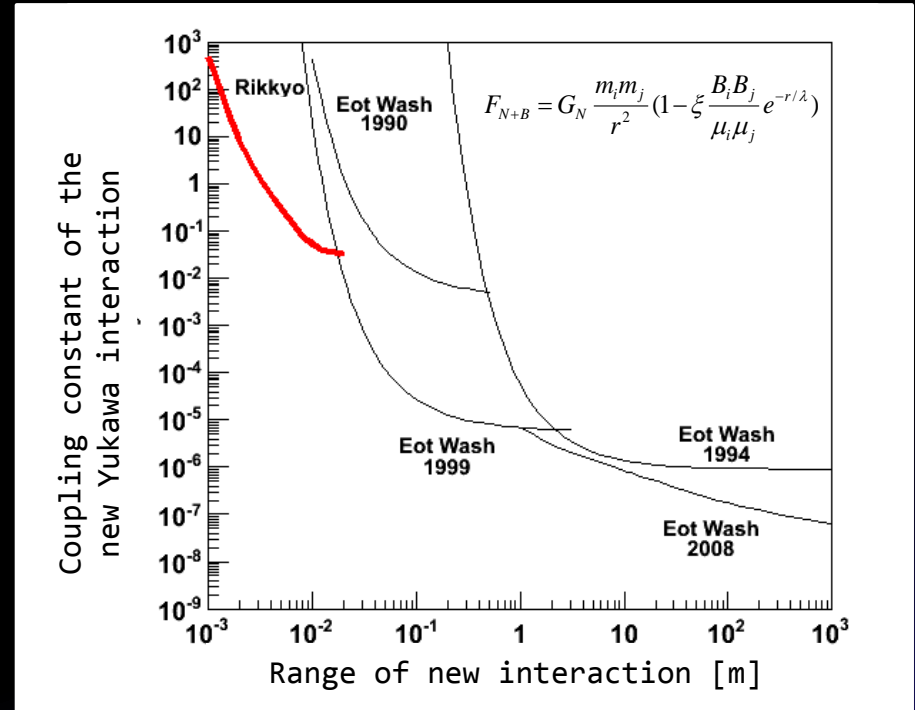
Result

Composition dependence of the gravitational constant



G_{Newton} : PDG value

Upper limit of the baryon number coupling force



First direct test below cm

$$\frac{G_{Al-W}}{G_{Cu-W}} = 1.009 \pm 0.010_{\text{stat}} \pm 0.048_{\text{syst}}$$

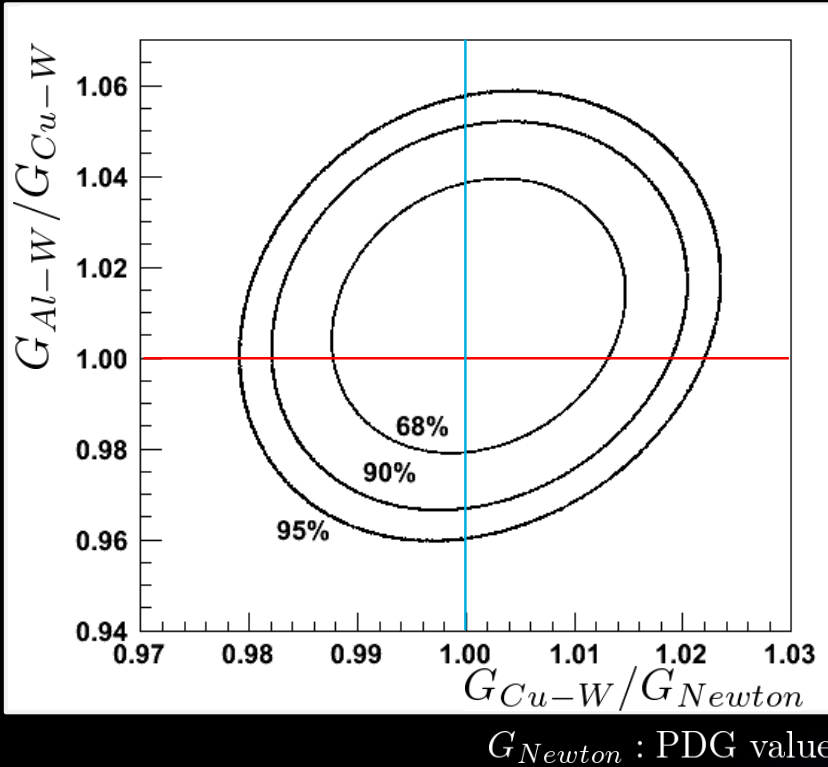
$$\frac{G_{Cu-W}}{G_{Newton}} = 1.001 \pm 0.007_{\text{stat}} \pm 0.021_{\text{syst}}$$

Center to center of 1.7 cm between attractor and target

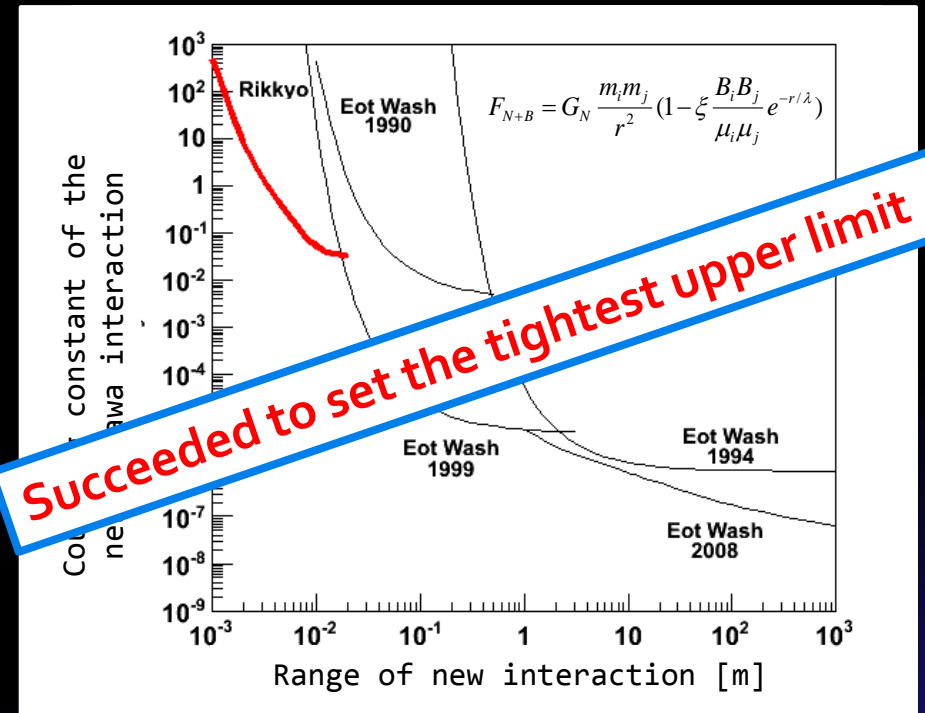


Result

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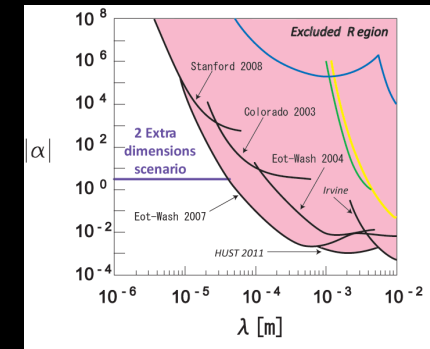
Center to center of 1.7 cm between attractor and target



Conclusion

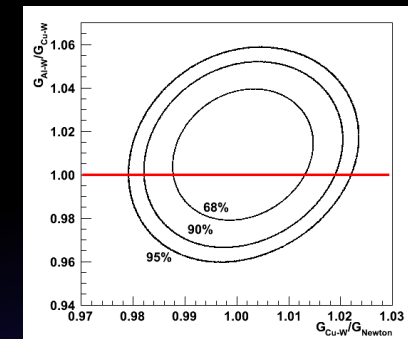
Test of the inverse square law

- Not contradicted with Newtonian inverse square law within our experimental precision at cm scale.



Test of the equivalence principle

- Confirmed the composition independence of the gravitational constant G at mm scale, **for the first time**.
- Succeeded to set the tightest upper limit of the baryon number coupling force below cm scale



The next Generation experiment

- Most precise test of Newtonian inverse square law below mm scale